

Here is a program that computes the left-hand sum, the right-hand sum, the midpoint sum, the trapezoid sum, and the Simpson sum approximations to the definite integral $\int_a^b f(x) dx$. The program displays the results together so that comparisons can be easily made. In the program, A and B are the limits of the integral, N is the number of subdivisions, and D plays the role of Δx . We store the left-hand sum in the variable L , the right-hand sum in R , the trapezoid sum in T , the midpoint sum in M , and the Simpson sum in S .

First you need to create a new program by pressing [PRGM] \rightarrow [NEW]. Give it a simple name such as ISUMS. Then carefully type in the following code, pressing [ENTER] at the end of each line. To type the variables $A, B, N, D, I, L, R, M, T, S$ use the green [ALPHA] keys. To type Y_1 press [VARS] \rightarrow [Y-VARS] \rightarrow [1:Functions] \rightarrow [Y_1]. The commands Prompt and Disp can be found by pressing [PRGM] \rightarrow [I/O]. The commands For and End are in [PRGM] \rightarrow [CTL]. The symbol \longrightarrow can be called by pressing the key [STO \rightarrow].

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Prompt N
Prompt A
Prompt B
(B - A)/N  $\longrightarrow$  D
0  $\longrightarrow$  R
0  $\longrightarrow$  M
For (I,1,N)
A + I * D  $\longrightarrow$  X
R +  $Y_1$  * D  $\longrightarrow$  R
X - D/2  $\longrightarrow$  X
M +  $Y_1$  * D  $\longrightarrow$  M
End
R + D *  $Y_1$ (A) - D *  $Y_1$ (B)  $\longrightarrow$  L
(L + R)/2  $\longrightarrow$  T
(2M + T)/3  $\longrightarrow$  S
Disp "L,R,T,M,S"
Disp L,R,T,M,S
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To execute the program, first store your function $f(x)$ in the Y_1 function variable, as you normally do when you want to graph $f(x)$. Then press [PRGM] and select ISUMS. At the prompts, enter the values for N, A , and B . The five approximating sums will be displayed on the home screen.